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11/11/2019

CAL

Custom Shelter on Mercer Island

File Name: I2258 Shelter on Mercer Island CAL1.xls

Calculation Note

"Engineers make conservative assumptions based on education and years of experience on their expertise. The engineer and I both agree on the assumptions on the loading of the beam and that the PCB-2 was clearly resisting the worst case loading condition. Stress calculations indicate that the wood beam was structurally adequate."

Building Code

2015 Washington Building Code

Building Category

II

Occupancy Type

Assembly A-5

ASCE

ASCE 7-10

Building Data

Shelter Width

20 ft

Shelter Length

40 ft

Post Spacing

10 st

CTB Width

5

CTB Length

16

CTB Span

16

CTB Weight

346

Shelter Mean Roof Height

15 ft

Roof Slope

6 /12

Footing depth

4.6 ft

Footing Diameter

3 ft

Soil Bearing

2000 psf

11/25/2019
For Sheets 1/22
through 22 of 22

Design Loads

Roof Dead Load (incl 4 psf for CTB and convert to horiz proj) RDL

18 psf

Roof Live Load RLL

30 psf

Wind Design Data

Basic Wind Speed	110	mph
Wind Exposure Category	C	
Wind Importance Factor	1.0	
Tributary Area	800	sf
K_h	0.85	
K_d	0.85	
K_{zt}	1.00	
Internal Pressure Coefficient	0.0	psf
$q_h =$	22.4	psf

	Load Case A	Load Case B
C_{nw} (page 67 of ASCE 7-10)	1.20	0.20
C_{nl} (page 67 of ASCE 7-10)	-0.10	-0.85
Vertical projection of roof along long side		150
Vertical projection of roof along short side		50
Wind Base Shears	V _{xx} 1.1	V _{yy} 3.4
		kips

Snow Load Design Data

Ground Snow Load	20	psf
Snow Exposure Factor	1.0	
Snow Importance Factor	1.0	
Snow Thermal Factor	1.2	
Flat Roof Snow Load	24	psf
Roof Slope Factor	1.0	
Sloped Roof Snow Load	RSL 24	psf

Seismic Design Data

Seismic Importance Factor	1.00	
Short Period Spectral Response Acceleration	S _s 1.408	
I-Second Period Spectral Response Acceleration	S _I 0.488	
Seismic Site Class	D	
Design Short Period Spectral Response Acceleration	S _{ds} 0.939	
Design I-Second Period Spectral Response Acceleration	S _{dI} 0.541	
Seismic Design Category	D	
Basic Seismic Resisting System		Cantilevered Column System
Basic Seismic Force Resisting System		Timber Frames
Response Modification Factor	1.5	
Seismic Response Coefficient	0.63	
Seismic Base Shear (Strength Design)	9.0	kips
Seismic Base Shear (Allowable Stress Design)	6.3	kips

Curved Tapered Beam Analysis

By inspection, PCB-2 will control the design of the two beam types. Also, by inspection, roof dead load + 30 psf roof live load will govern over snow, wind or seismic for the beam design.

Input

PCB-2

Southern Pine

Span	L	16.0	ft	LDF	1.25
Spacing	S	10.0	ft	Fb	2400 psi
Roof Slope (x/12)	P	6.0		Fv	200 psi
Dead Load	DL	18.0	psf	E	1800000 psi
Live Load	LL	30.0	psf		
Allowable Deflection	D	0.800	in (L/240)		
Width	B	5.000	in		
Vertical End Depth	De	7.688	in		
Vert Centerline Depth	Dc	30.375	in		
Centerline Str Depth	Dcs	16.000	in		
Radius	R	16.000	ft		
Lam Thickness	LT	1.375	in		

Intermediate Calculations

Roof Slope	phiT	0.464	radians
Curvature Factor	Cc	0.897	
Effective Length for Shear	Le	14.7	ft

Iterative Procedure to Calculate slope at bottom of Beam

1. Enter an assumed value of phiB,
2. Compare with the calculated value of phiB,
3. Enter a closer approximation of phiB
4. Repeat until phiB (assumed) = phiB (calculated)

Assumed value for phiB

26.300 degrees

Assumed
Calculated

Compare these --->
Two values ----->

phiB
0.459 radians
0.459 radians

Curved Beam Geometry

Horizontal distance from tangent to tangent	Lc	14.18	ft
Horizontal distance from end to tangent	Lt	0.91	ft
Overall height of beam	Ha	4.64	ft
Height from bottom of beam to bottom of curve @ CL	Hs	2.11	ft
Vertical depth at tangent	Dt	7.75	in
Radius @ mid-depth at beam centerline	Rm	17.27	ft
Effective depth of beam for deflection	Deb	11.85	in

Shear and Moment Calculations

Uniform load on beam	W	480	plf
Shear at end of beam	Rv	3840	lbs
Moment at tangent	Mt	3299	ft-lbs
Moment at beam centerline	Mc	15360	ft-lbs

Stress Factors

Radial stress factor	Kr	0.146	
Bending stress factor	Ktheta	2.426	
Radial stress reduction factor	Cr	0.740	

Stress and Deflection Calculations

ENGR CHECK

Shear

Area at end of beam for shear stress	38	in^2
Actual shear stress	138	psi
Allowable shear stress	250	psi

OK

Bending at Tangent

Tangent depth perpendicular to lams	6.9	in
Section modulus	40	in^3
Actual bending stress	984	psi
Allowable bending stress	2826	psi

OK

Bending at Centerline, Structural Depth

Structural depth at beam centerline	16.0	in
Section modulus	213	in^3
Actual bending stress	864	psi
Allowable bending stress	2608	psi

OK

Bending at Centerline, Full Depth

Vertical centerline depth

30.4	in
769	in ³
582	psi
2429	psi

OK

Section modulus

$$K\theta * Mc^* 12/S$$

Actual bending stress

$$LDF * Cf * Cc * Fb$$

Allowable bending stress

$$2429 \text{ psi}$$

Radial Stress at Centerline

Bending stress

240	psi
26	psi
83	psi

OK

Actual radial stress

$$Kr * Cr * fb$$

Allowable radial tension

$$LDF * Fv / 3$$

Vertical Deflection at Centerline

Effective moment of inertia

$$B * De b^{3/12}$$

694	in ⁴
1	in
1	in

OK

Actual deflection at centerline

$$5WL^4 / (384EI)$$

Allowable deflection at centerline

H	3.4	ft
	0.2	in

Horizontal Deflection at Support

Height at mid-depth of centerline

Horizontal deflection at each end $(2 * H / L) * DEF_Lcl$

PI, P2, P3

Actual Width	3.000	in	Dead Load	18	psf	
Actual Depth	6.875	in	Live Load	30	psf	
Area	18	in ²	LDF	1.25		
Section Modulus	16	in ³	F _v	0.300	ksi	
Moment of Inertia	59	in ⁴	F _b	2.400	ksi	
Spacing	4.0	ft	E	1800	ksi	
Span	10.0	ft	Eave Cut	1.50	in	
Total Load	0.192	klf	Neutral Axis	3.08	in	
End Reaction	1.0	kips	Vol Factor	1.00		
Shear	0.9	kips	W(klf)			
Moment	2.4	ft-kips	^ ^			
Deflection	0.41	in	^ ^			
<hr/>						
Shear Stress	<u>Actual</u>		<u>Allowable</u>		<u>Status</u>	
	0.069		0.375		OK	
Bending Stress	1.848		3.000		OK	
Total Deflection Ratio	296		240		OK	

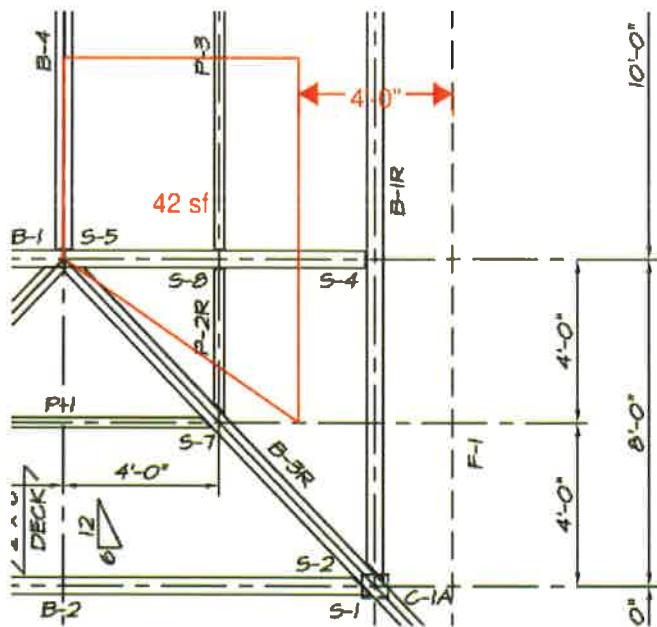
B1

Tributary area for point load into B1

42 sf

Tributary width for distributed load into B1

4.0 ft



Actual Width

5.000 in

Dead Load

18 psf

Actual Depth

13.750 in

Live Load

30 psf

Area

63 in^2

LDF

1.25

Section Modulus

111 in^3

Fv

0.300 ksi

Moment of Inertia

830 in^4

Fb

2.400 ksi

Span

18.0 ft

E

1800 ksi

Spacing

4.0 ft

Eave Cut

2.50 in

P

2.0 kips

Neutral Axis

6.27 in

a

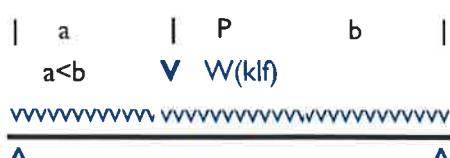
8.0 ft

Vol Factor

1.00

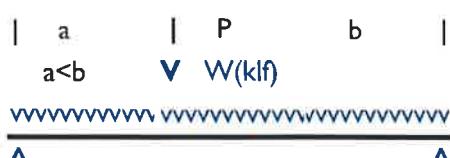
b

10.0 ft



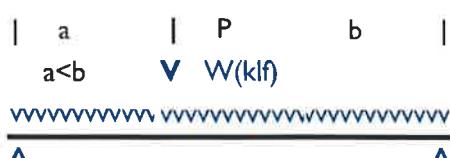
Uniform Load

0.192 klf



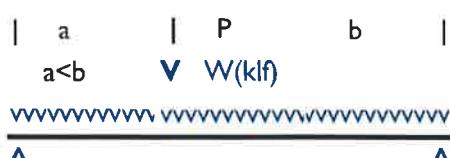
Ryl

2.9 kips



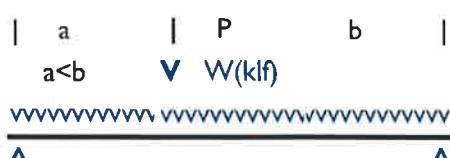
Ryr

2.6 kips



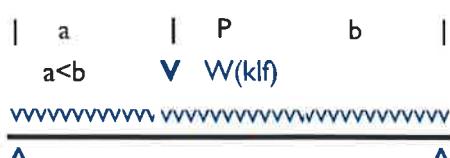
Shear

2.6 kips



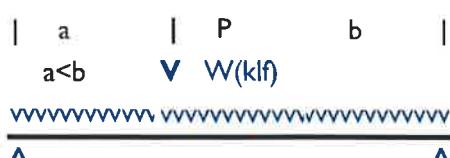
Ma

10.0 ft



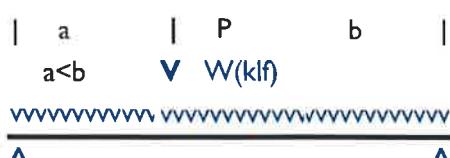
Moment

16.7 ft-k



Deflection

0.58 in



Shear Stress

Actual

0.063

Allowable

0.375

Status

OK

Bending Stress

Actual

1.802

Allowable

3.000

Status

OK

Deflection Ratio

Actual

372

Allowable

240

Status

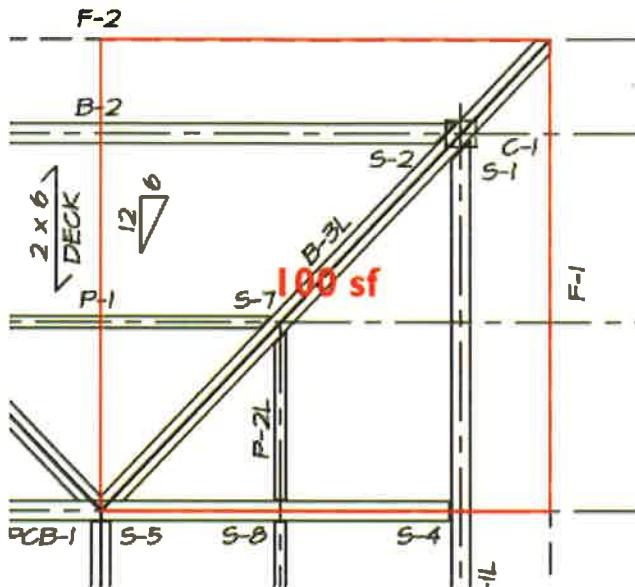
OK

B2

Actual Width	5.000	in	Dead Load	18	psf
Actual Depth	13.750	in	Live Load	30	psf
Area	63	in ²	LDF	1.25	
Section Modulus	111	in ³	F _v	0.300	ksi
Moment of Inertia	830	in ⁴	F _b	2.400	ksi
Spacing	6.0	ft	E	1800	ksi
Span	16.0	ft	Eave Cut	2.50	in
Total Load	0.288	klf	Neutral Axis	6.27	in
End Reaction	2.3	kips	Vol Factor	1.00	
Shear	2.0	kips	W(klf)		
Moment	9.2	ft-kips	vvvvvvvvvvvvvvvvvvvvvvvvvvvvvvv		
Deflection	0.28	in	^ ^		
Actual					
Shear Stress	0.047		Allowable	0.375	
Bending Stress	0.996			3.000	
Total Deflection Ratio	675			240	
Status					
OK	OK	OK			

B3

Calculations below will show that this beam is very conservatively designed so the total load on the beam will be approximated as a uniform load.



Total square feet supported by beam	100 sf
Beam span + cantilever	14.1 ft
Equivalent uniform load	7.1 ft

Actual Width	5.000	in	Pitch	4	/12	
Actual Depth	11.000	in	Dead Load	18.0	psf	
Area	53.0	in ²	Live Load	30.0	psf	
Section Modulus	87.2	in ³	P	0.0	kips	
Moment of Inertia	496.8	in ⁴	a	2.8	ft	
Total Load	0.339	kif	Eave Cut	0.81	in	
Span	11.3	ft	Neutral Axis	5.30	in	
Spacing	7.1	ft	Vol Factor	1.00		
Ryl	1.8	kips	LDF	1.25		
Ryr	3.0	kips	F _v	0.300	ksi	
Ma	5.3	ft	F _b	2.400	ksi	
Moment @ Ma	4.8	ft-k	E	1800	ksi	
Moment @ Ryr	1.4	ft-k	P			
Vmax	2.0	kips	W(kif)			
Mmax	4.8	ft-k	V			
Defl @ L/2	0.13	in	^ A L a			
Defl @ O'hang	-0.09	in				

Design Check

Shear Stress
Bending Stress
Deflection

Actual	Allowable	Status
0.058	0.375	OK
0.657	3.000	OK
1015	240	OK

B4

Actual Width
Actual Depth
Area
Section Modulus
Moment of Inertia
Spacing
Span
Total Load
End Reaction
Shear
Moment
Deflection

5.000	in
6.875	in
31	in ²
28	in ³
104	in ⁴
4.0	ft
10.0	ft
0.192	klf
1.0	kips
0.9	kips
2.4	ft-kips
0.23	in

Dead Load
Live Load
LDF
Fv
Fb
E
Eave Cut
Neutral Axis
Vol Factor

18	psf
30	psf
1.25	
0.300	ksi
2.400	ksi
1800	ksi
1.25	in
3.14	in
1.00	

W(klf)

Shear Stress
Bending Stress
Total Deflection Ratio

Actual
0.041
1.038
519

Allowable
0.375
3.000
240

Status
OK
OK
OK

C1, C2

Loading combination that controls is dead load + seismic load on C2. Seismic force will be in a direction to create weak axis bending. Check for dry conditions of use.

Axial Load on C2

2.4	kips
1.1	kips
10.2	ft
10.7	ft-k

Lateral load at top of C2 (seismic base shear / 6)

Column length above base

Moment at base of column

Width

6.750	in
8.250	in
10.2	ft
1.60	
1.650	ksi
1.600	ksi
1.800	ksi
1700	ksi
2.4	kips
0.0	ft-kips
10.7	ft-kips

Depth

Span

LDF

F_c

F_b in strong axis

F_b in weak axis

E

P_{max}

M_{max} in strong axis

M_{max} in weak axis

Compression

Compression stress

0.044	ksi
0.418	
0.90	
2.1	
38.1	
2.640	ksi
0.490	ksi
0.182	
0.091	

Coefficient that depends upon coefficient of variation

Coefficient for solid sawn, glulam or round piles

Buckling length coefficient

Length divided by width or depth, depending on which controls

Allow F_c stress multiplied by all adjustment factors except C_p

Buckling strength of column

Column stability factor

Compression portion of unity check

Strong Axis Bending

Section modulus

77	in^3
0.000	ksi
1.00	
2.560	ksi
0.490	
0.000	

Strong axis bending stress

Volume factor

Allowable bending stress with adjustments for LDF and C_v

F_{cE1}

Strong axis bending portion of unity check

Weak Axis Bending

Section modulus

63 in³

Weak axis bending stress

2.055 ksi

Allowable bending stress with adjustments for LDF

2.880 ksi

F_{cE2}

0.490

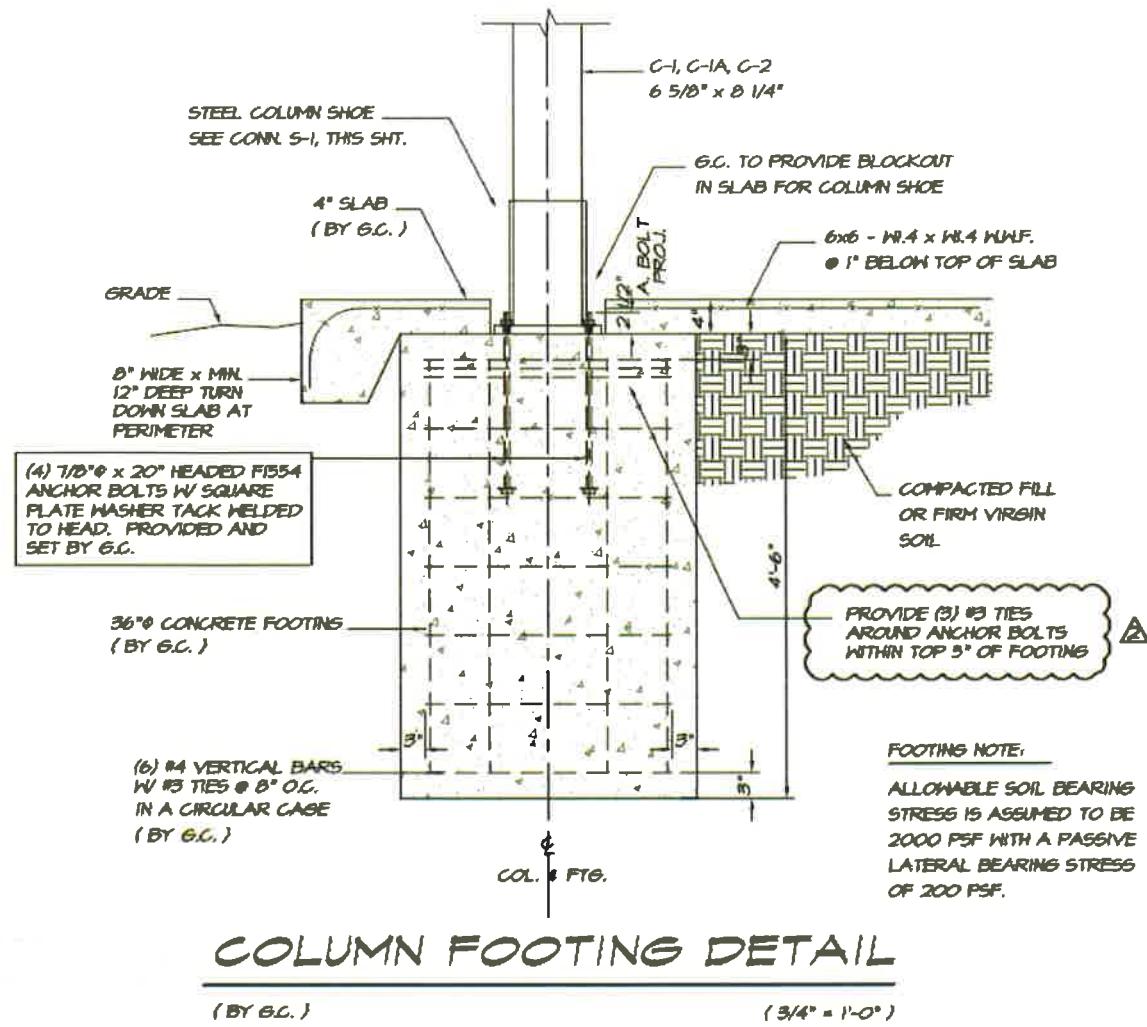
Weak axis bending portion of unity check

0.783

Total

0.874

Concrete Footing



Design with Constraint at the Ground Surface

Allowable lateral soil bearing pressure per foot from Table 6.6

Applied horizontal force on pole

Height above ground at which force P is applied

Diameter (or width) of concrete casing

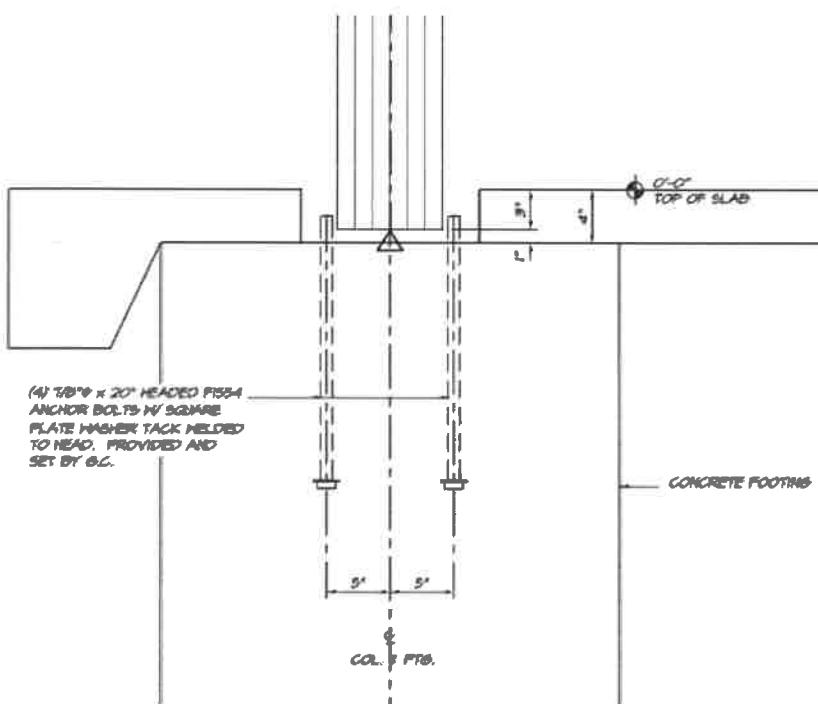
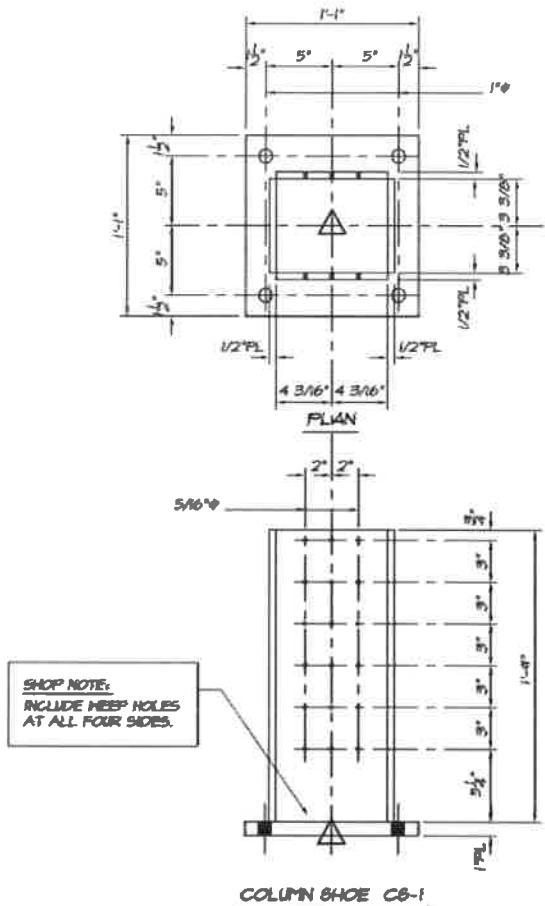
Required depth of embedment

Actual embedment depth

Status

S_0	400	lbs/sqft/ft
P	1052	lbs
h	11	ft
B	3.00	ft
d reqd	3.5	ft
	4.5	ft
OK		

Conn SI



Maximum axial load (dead load + live load)
Maximum axial load (seismic)
Maximum moment (seismic)

6.5	kips
1.1	
10.7	ft-k

Check Anchor Bolts

Moment arm on anchor bolts
Tension force per anchor bolt
Allowable tension per 7/8" diameter anchor bolt

10	in
6.4	kips/AB
11.5	
OK	

Check Bearing Stress

Shoe height
Moment arm (assume 2" uniform bearing top and bottom)
Bearing width
Bearing stress
Basic allowable bearing stress
Wet use factor
Load duration factor
Adjusted allowable bearing stress
Status

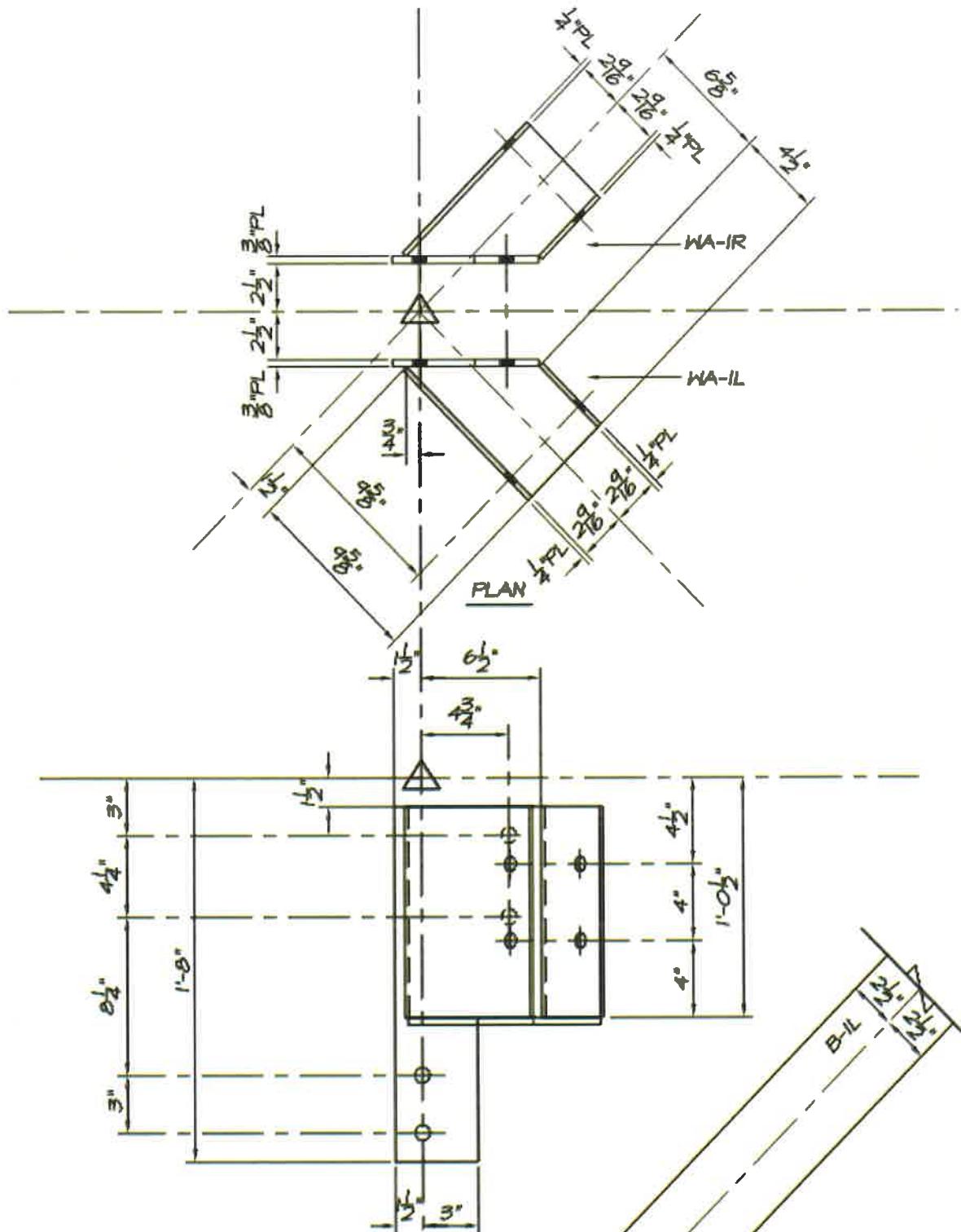
21	
17	
8.25	
0.459	ksi
0.650	ksi
0.53	
1.60	
0.551	
OK	

Check Uplift

Dead Load (Use 0.6 * 10 psf = 6 psf)
Wind uplift
Net wind uplift
Tributary area to one column
Total wind uplift on one column
Basic allowable load per Simpson 2 1/2" SDS screw
By inspection, (36) screws are OK.

6.0	psf
-22.4	psf
-16.4	psf
192	sf
-3.1	kips
0.42	kips/screw

Conn S2



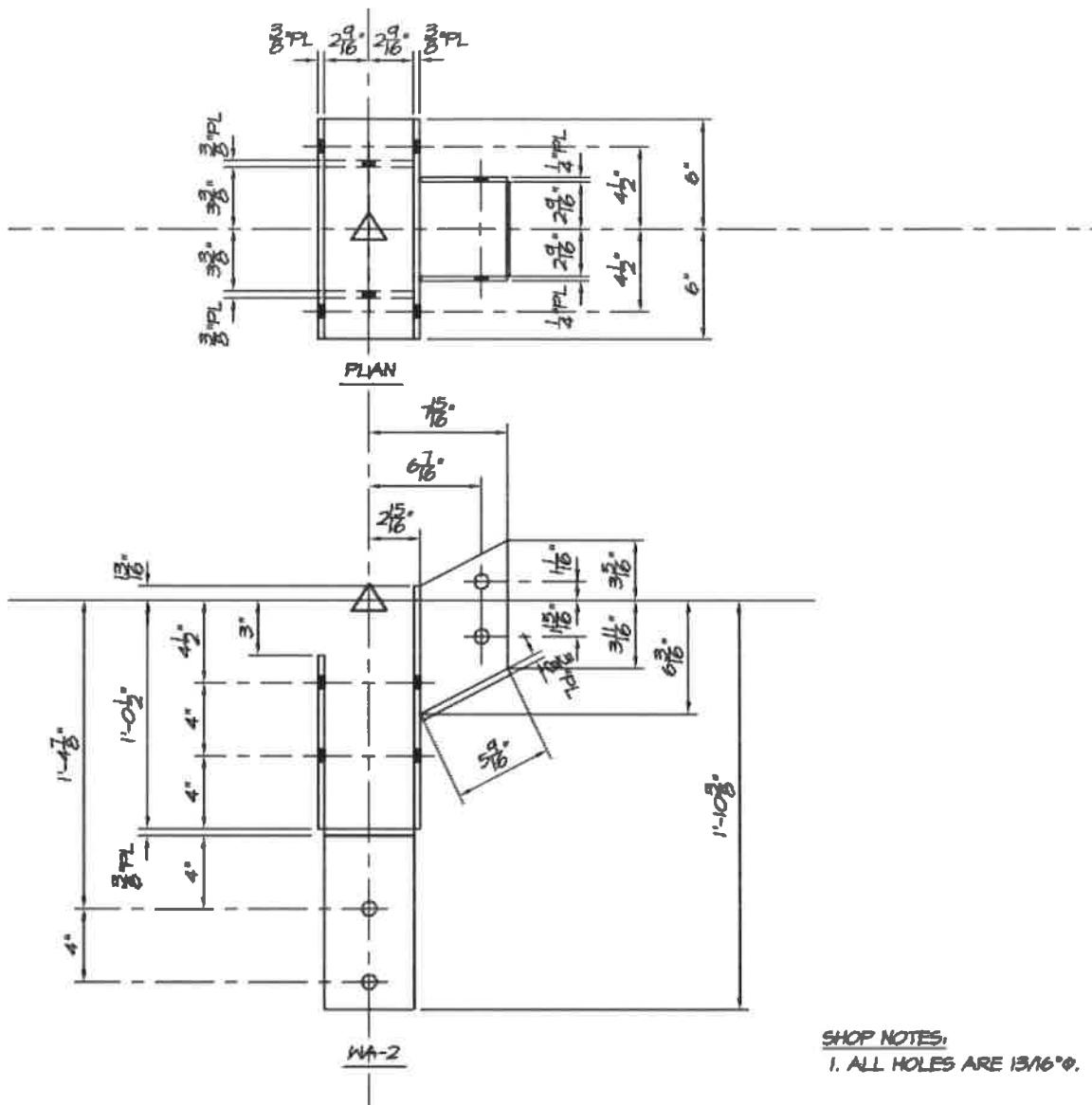
Maximum gravity load per B2

Maximum uplift load on column

Connection is OK by inspection

2.3	kips
-3.1	kips

Conn S3



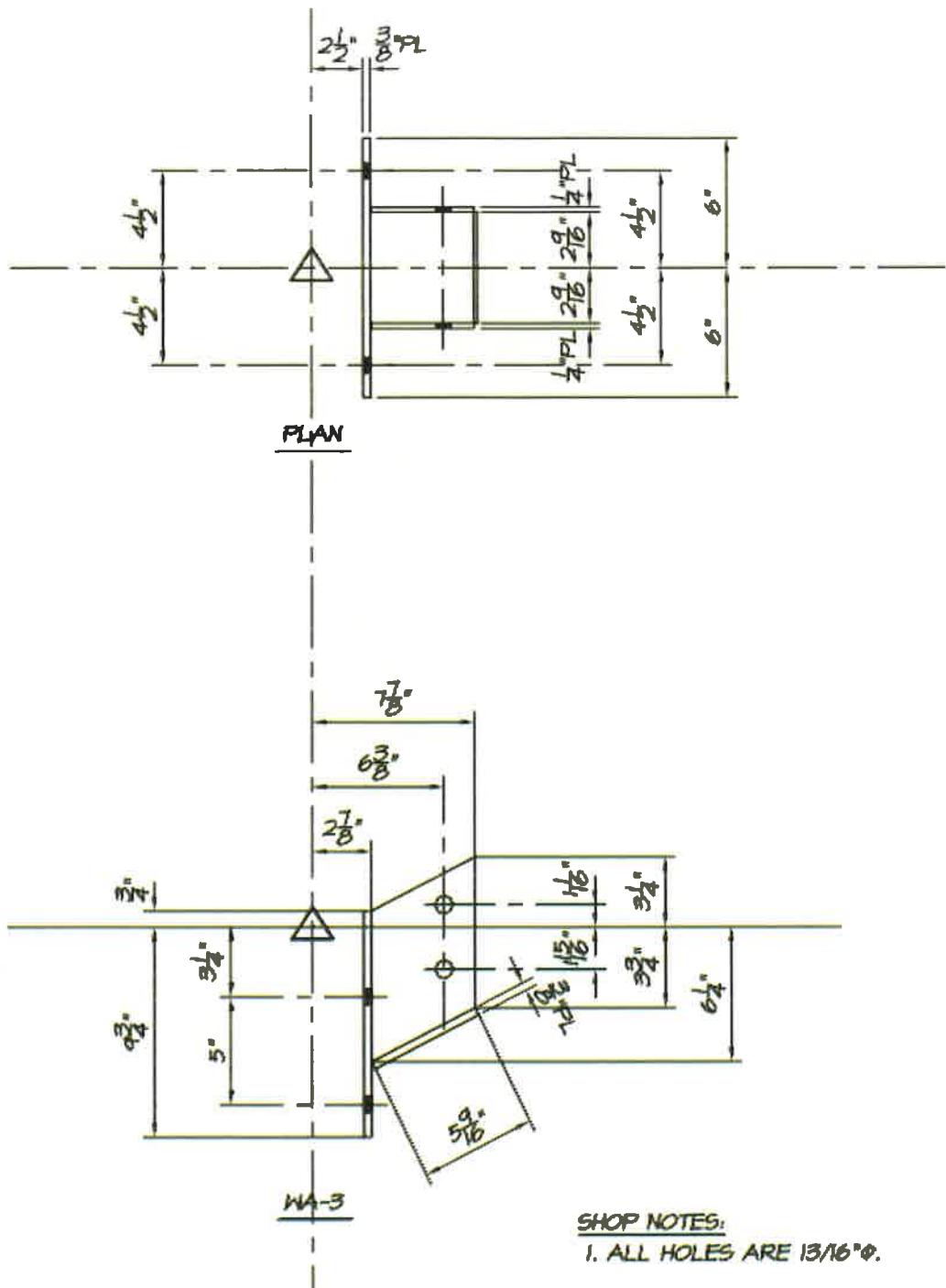
Maximum gravity load per B2

Maximum uplift load on column

Connection is OK by inspection

9.1	kips
-3.1	kips

Conn S4



Maximum reaction from CTB

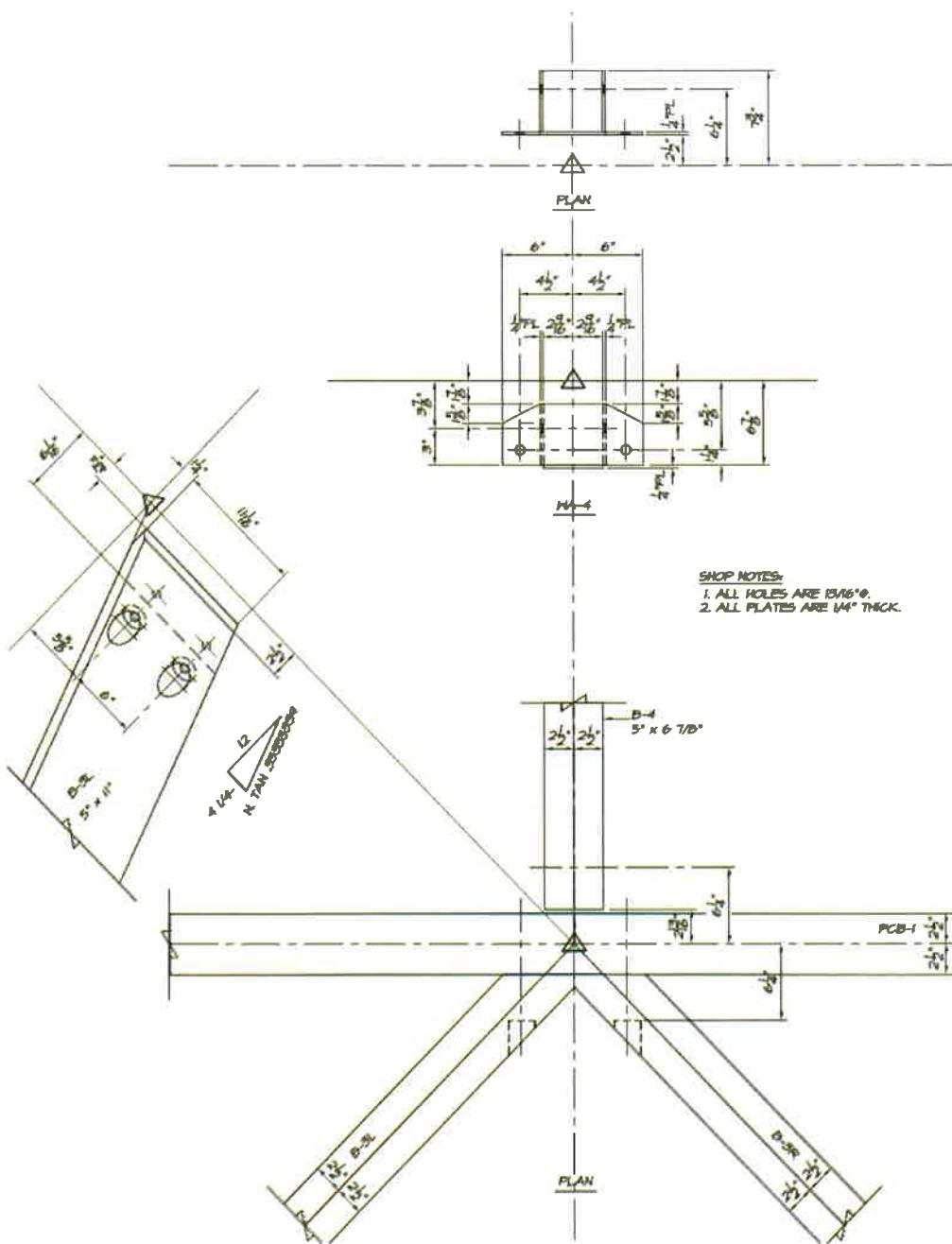
Basic allowable load for 3/4" diameter bolt at 90 degrees, single shear

Allowable for (4) bolts with 1.25 load duration factor

Status

3.8	kips
1.00	kips/bolt
5.0	kips
OK	

Conn S-5



B3 reaction

B4 reaction

The shoe for B4 with (2) bolts in back plate is ok by inspection.

Basic allowable load for 3/4" bolt in single shear at 90 degrees to grain

Reduction for end grain

Allowable load for (4) bolts with 1.25 load duration factor

Status

1.8 kips

1.0 kips

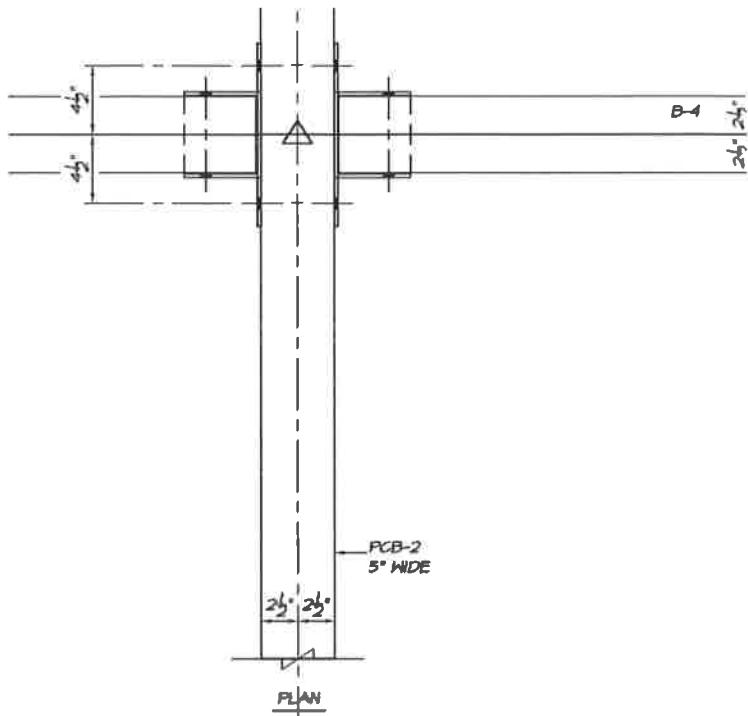
066

06

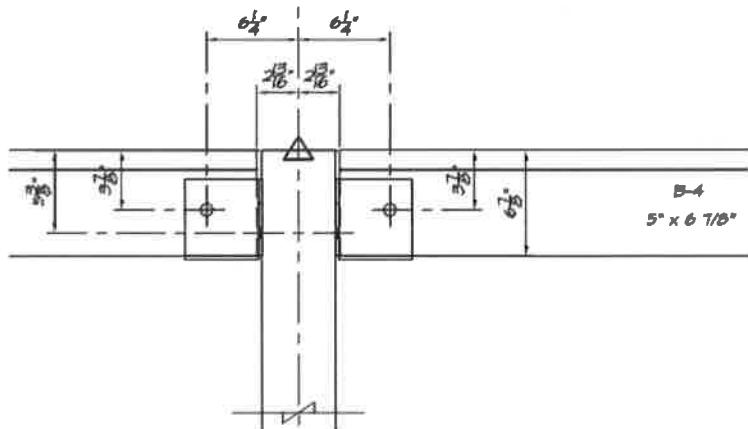
2.0

OK

Conn S6



SHOP NOTES:
1. ALL HOLES ARE 13/16".

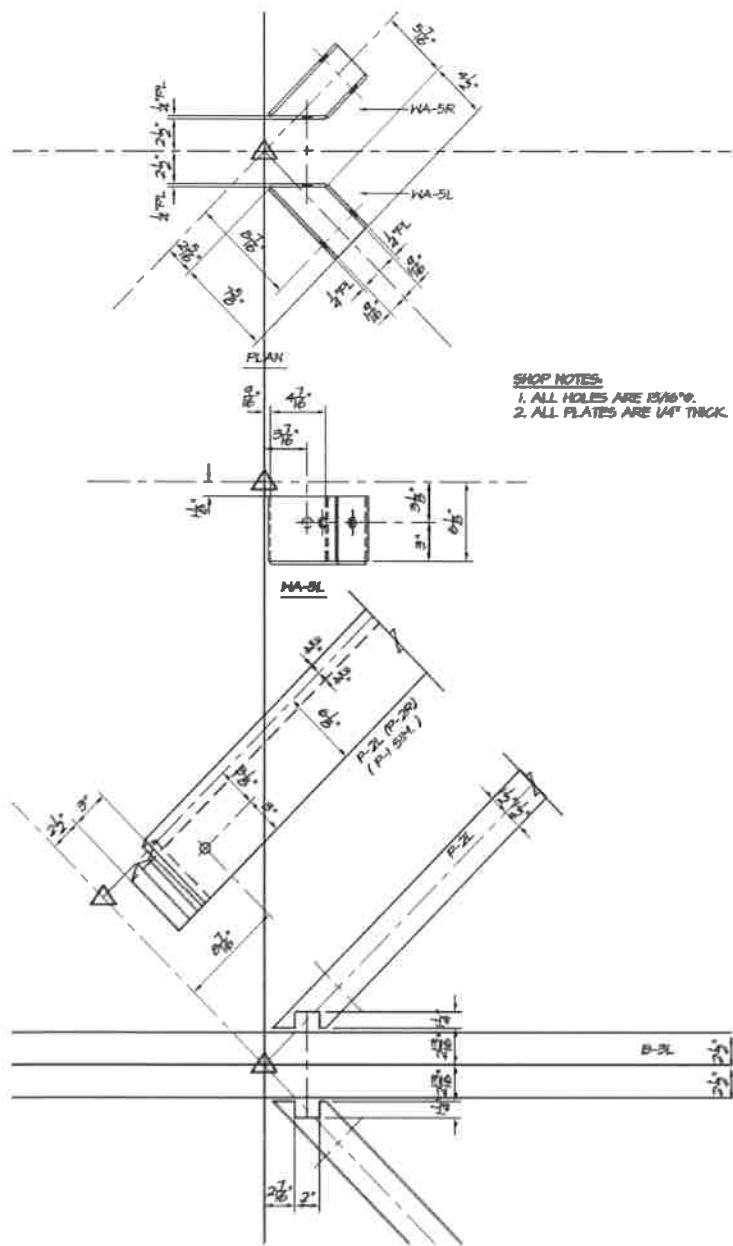


B4 reaction

OK by inspection per calculation above.

1.0 kips

Conn S7

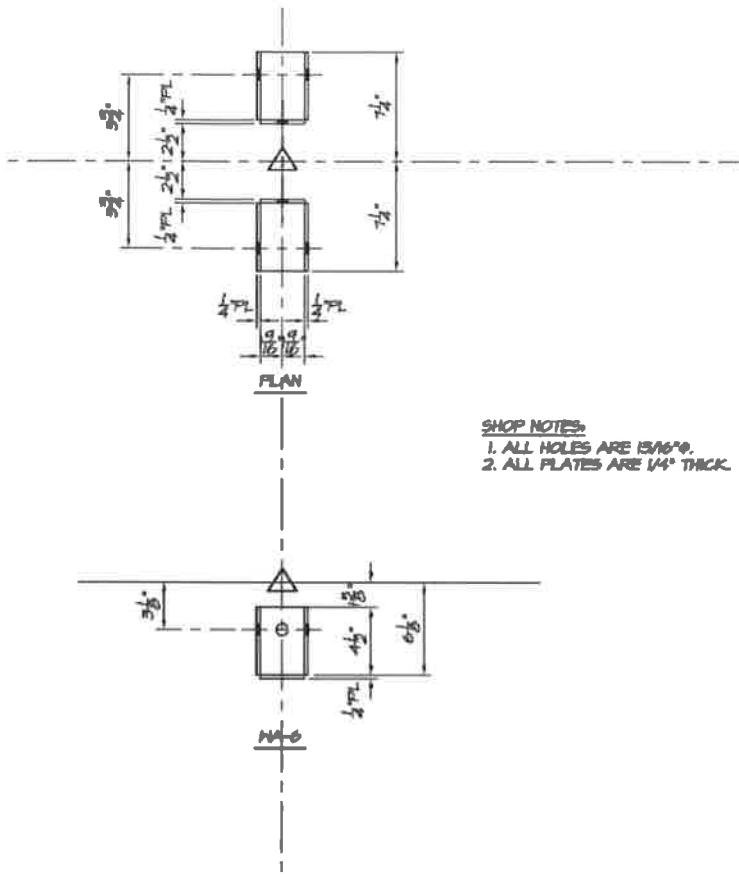


P1 reaction

0.8 kips

OK by inspection

Conn S8



SHOP NOTES
1. ALL HOLES ARE 13/16".
2. ALL PLATES ARE 1/4" THICK.

P3 reaction

1.0 kips

OK by inspection



DANIEL C. SMITH PROFESSIONAL ENGINEER				
13237 Melvin Arnold Rd Raleigh N.C. 27613 919-844-6050	5/21/2019			
DCSPE Job#	7196			
Project Zip Code	98040			
City, State	Mercer Island			
Building Design				
Building Code	2018			
Building Category	II			
Occupancy Type	Assembly A-5			
ASCE	ASCE 7-10			
Overall Width	20.0 ft			
Overall Length	40.0 ft			
Post Spacing	10.0 ft			
CTB Width	5.0 in			
CTB Length	16.0 ft			
CTB Span	16.0 ft			
CTB Weight	346.0 lbs			
Mean Roof Ht	15.0 ft			
Roof Slope	6 :12			
Footing Depth	4.6 ft			
Footing Diameter	3.0 ft Ø			
Soil Bearing	2000 psf			
Design Loads				
Roof Dead Load	12 psf			
Roof Live Load	30 psf			
Wind Design Data				
Wind Speed	110 mph			
Exposure	C			
Imp wind	1.00			
Tributary Area	80.0 ft^2			
Kh	0.85			
Kd	0.85			
Kzt	1			
Internal Pressure Coefficient	0.00			
Components & Cladding Wind Pressures	Z1 Z3	-12.1 psf -58.2 psf	Z2	-38.0 psf
qh =				22.38
Wind Base Shears	Vxx	1.5 kips	Vyy	2.9 kips



SNOW DESIGN DATA		
Snow (Pg)	20.0 psf	
Snow Exposure (Ce)	1.00	
Imp Snow (Is)	1.00	
Snow Thermal (Ct)	1.2	
Flat Roof Snow Load (Pf) (.7 IS USED FOR FNEAR FLAT ROOFS ONLY)	24.0 psf	
Roof Slope (Cs)	1.00	
Sloped Roof Snow Load (Ps)	24.0 psf	

SEISMIC DESIGN DATA

Seismic Importance Factor (Ie)	1.00
Short Period Spectral Response Accel (Ss from maps)	1.443
1-Sec Period Spectral Response Accel (S1 from maps)	0.488
Seismic Site Class	D
Design Short Period Spectral Response Accel (Sds)	0.96
Design 1-sec Period Spectral Response Accel (Sd1)	0.49
Seismic Design Category	D
Basic Seismic Resisting System	CANTILEVERED COLUMN SYSTEM
Basic Seismic Force Resisting System	TIMBER FRAMES
Response Modification Factor (R)	1.5
Seismic Response Coefficient (Cs)	0.64
Seismic Base Shear (Allowable Stress Design)	0.00

Connection Design Data

Plate Thickness	0.50 in
Screw diameter	0.25 in
# of Screws per Post	36
Max Allowable Force per Bolt	230
Shear of Tube Steel	36000 psi
Width of Post	5.0 in
Length of Post	5.5 in
Bearing Pressure of CTB	



Roofing Board Data

Width of Roofing Board	5.5 in
Height of Roofing Board	1.5 in
Maximum Span of Board	10.0 ft
Modulus of Elasticity	1600000
Cd	1.15
Fb (allowable bending stress)	1350.0 psi



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05/22/19

Project: DCSPE #: 7196
Subject: Shelter Calculations

Mercer Island, WA

D. C. Smith
5/22/19

1. Scope

Daniel C. Smith PE Consulting Engineers (DCSPE) was contacted by SWS , regarding load calculations.

2. Design Codes

2018 International Building Code

Occupancy Type:	Assembly A-5	Wind Speed:	110 mph
Construction Type:	II	Wind Importance:	1.00
Building Height:	15.0 ft	Exposure:	C
Soil Bearing Capacity:	2000 psf	Snow Load:	20 psf
Seismic Category:	C	ASCE 7-10	

3. Design Loads

Dead Load

CTB Load = 346 lbs each / (10 x 8 ft) =	4.3 psf
DLr = 12 + CTB 4.3 psf =	16.3 psf

Live Load roof (LLr) =	30.0 psf
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Wind Load

V (Allowable) =	110 mph
Open Structure = 1 = 1 = 0.85 = 0.85	= 15 ft

qh = 0.00256 * Kzt * Kd * Kh * 110^2 =	22.4 psf
	EnWood uses WL (up) 20 psf.

WL (down) 10 psf	Conservative	10.0 psf
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Snow Load	
Pg =	20.0 psf
Exp C - fully Exposed Imp = 1 Ct = 1.2	
Flat Roof Snow Load (Pf) = .7 * 20 * 1 * 1.2 * 1	24.0 psf
Cs = 1 (Roof Slope: 6:12)	
Sloped Roof Snow Load (Ps) = 1 x 24	24.0 psf
4. Load Combinations	
DL - 0.6WL = 16.3 - .6*22.38 =	4.3 psf down
.75 (DLr + WLdown) = .75 (16.3 + 110) =	19.7 psf
DLr + .75(.6WLdown+LLr) = DLr + .75(.6*10 + 30) =	43.3 psf
DLr + .75(.6WLdown+SL) = DLr + .75(.6*10 + 24) =	38.8 psf
DLr + LLr = 16.3 + 30 =	46.3 psf
DL + SL = 16.3 + 24 =	40.3 psf
Worst Case Scenarios	
Use downward pressure of	46.3 psf
Use wind uplift pressure of	4.3 psf
(There is no uplift loads)	
5. Calculations	
CTB Gravity Loads to Column (Shear)	
46.3 psf x 10 ft x 16 ft/2 =	3704 lbs
Wood bears on 0.5" thick steel plate 5 x 5.5 x 650 =	17875 lbs
36 - 0.25" bolts - 3.16" thick steel	<= 1.0 = OKAY
Shear of metal tube steel psi x .4 x .187: x 36 faces x 36 bolts =	10771 lbs
	<= 1.0 = OKAY
	0.344
Check Screws (Uplift)	
Uplift Pressure	Uplift check with 25 psf 25
Uplift Force Total	2000
Quantity of Screws	36
Force per Screw	55.56
Maximum Allowable Force per Screw	230
	<= 1.0 = OKAY
	0.242



Check Bolts (Uplift)

Uplift Pressure	Uplift check with 25 psf	25
Uplift Force Total		2000
Quantity of Bolts (5/8" diameter)		2
Force per Bolt		1000.00
Max Allowable Force per Bolt (NDS Parallel to Grain)		1900
	<= 1.0 = OKAY	0.526

Check footings

Calculated load

Tributary area supported by each post is 10 ft * 16 ft/2 =	80.0 ft^2
Volume of Footing =	32.52 ft^3
Weight of Footing =	4877 lbs
46.3 psf x 80 ft^2 = 3704 lbs + Weight of Footing =	8581 lbs

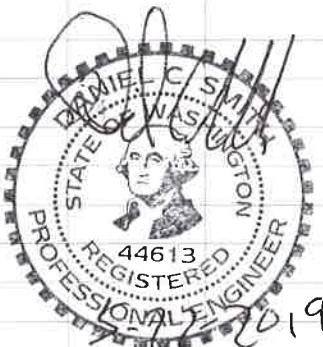
Calculated soil resistance

2000 psf soil bearing x (3 ft Ø)^2 x Pi/4 =	14138 lbs
	<= 1.0 = OKAY
	0.607
Required Area of Footing = Calculated Load / Soil Bearing =	4.29
Provided Area of Footing = (Footing Diameter^2 * Pi) / 4	7.07
	<= 1.0 = OKAY
	0.61

Wind Uplift is negligible.

7. Check Roof Deck Boards

2x6 Tongue and groove boards - SYP #1	1.55 in^4
Modulus of Inertia (I) = $5.5 \times 1.5^3/12$ =	2.06 in^3
Section Modulus (S) = $5.5 \times 1.5^2/6$ =	
Worst case load combination is =	46.3 psf
Uniform load per board (w) = $46.3 \times 5.5 \text{ in}/(12 \text{ in}/\text{ft})$	21.2 plf
Cd =	1.15
Bending Stress	10' Span
Moment (M) = $w \cdot L^2/8$ ft x 12 in/ft	3180.0 lbs-in
fb (bending stress) = $M/(S \cdot Cd)$	1340.7 psi
Fb (allowable bending stress) =	1350.0 psi
	<= 1.0 = OKAY
	0.993



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Project Name: Mercer Island Wa **DCSPE 7196**
Location: Mercer Island Wa

Curved Taper Beam Calculation

Material Properties

F _b	2400	psi	F' _b	2275.62	psi
F _v	200	psi	F' _v	223	psi
F _{rt}	66.67	psi	F' _{rt}	67.08	psi
C _m	0.97		C _{fbend}	0.84	
C _d	1.15		C _{ftan}	0.88	
C _f	1		C _r	0.85	
E _y	1800000		E'	1620000	psi



Structural Dimensions

Length/Span (L)	16	ft	(I)	192	in
Trib Width/Spacing	10	ft		120	in
Top Pitch/Slope (P)	6	:12		26.57	degrees
A=	0.135		D=	2.76	
B=	0.060		E=	-2.7554426	
C=	0.120		F=	3.19	

Estimated Beam Size

width/b	5	in	vert end depth/de	7	in
Radius (R)	16	ft	vert CL depth/dc	30	in
	192	in			

Structural Loads

DL=	20	psf	w=	500	plf
SL=	15	psf			
LL=	30	psf			

Stress Factors

Radial Stress Factor	K _r	0.1462944	A+B(dc/Rm*12)+C(dc/Rm*12)^2
Bending Stress Factor	K _{theta}	2.43	D+E(dc/Rm*12)+F(dc/Rm*12)^2
Radial Stress Red Factor	C _r	0.9371981	

Design of CTB

1. Determine minimum end depth

SHEAR AT END OF BEAM	R _v =	4000	lbs	wL/2	OK
UNADJUSTED END DEPTH?	d=	5.4	in	3R _v /2bF' _v	
EFFECTIVE LENGTH FOR SHEAR	L _e =	15.1	ft	L-2d	
SHEAR BASED ON EFFECTIVE LENGTH	V=	3776	lbs	wL _e /2	
MINIMUM END DEPTH	d _e =	5.1	in	3V/2bF' _v	

2. Determine approximate trial centerline depth dc_b from the bending stress limitation

M=	192000	in-lb	wL ² /8
F' _b =	2275.62	psi	F _b *C _f
dc _b =	16.7	in	sqrt(6MD/bF' _b)

3. Determine trial minimum centerline depth dc_{delta} from the deflection limitation

deltamax	1.07	in	l/180
deff=	4.56	in	((Wl ³)/(6.4*E'*b*deltamax*cosT ³))^(1/3)
dc _{delta} =	4.0	in	2deff-de

4. Determine trial minimum centerline depth dc_r from radial stress limitation.

dc _r =	22.4	in	sqrt(6MK _r /bF' _r t)
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To reduce depth design for radial reinforcement, using maximum radial tension stress F_v/3

dc _r =	21.0	in	sqrt(6MK _r /(b(F _v /3)*1.15))
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5. Determine height of apex ha, trial bottom slope theta_B, and soffit radius R

HEIGHT OF APEX POINT	ha=	4.58	ft
LARGEST DEPTH	dc=	30.0	in
HEIGHT OF SOFFIT MIDSPAN	hs=	2.08	ft
MAXIMUM BOTTOM SLOPE	max bot slo	29.19	°
MAX EFFECTIVE BOTTOM SLOPE	thetaB max	26.6	°
MINIMUM BOTTOM SLOPE	thetaB min	25.3	°
TRIAL BOTTOM SLOPE	trial bot slo	25.3	°
EFFECTIVE SOFFIT RADIUS	R=	17.25	ft

6. Find the following values based on the values of theta_B and R determined in step 5

a) length of tapered leg

lt=	14.04	in	l/2 - RsinB	Lt	1.1 ft
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b) Ratio of Span Length to distance between tangent points

lc=	163.9	in	l - 2lt	Lc	13.66 ft
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c) Depth of beam at tangent points

dt=	7.4	in	de + lt(tanT - tanB)
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d)

Rm=	17.3	in	R+DC/24
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dc/Rm=	1.74
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e)

ftheta=	256	psi	6M/bdc ²
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7. Check maximum deflection

deb=	12.1	(de+dc)(0.5+0.735*tanT)-(1.41dctanB)
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deltaC=	0.55	in	5WI ³ /32E'bdeb ³
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1.06 > 0.55 = OK

8. Check stresses**a) Bending stress at centerline**

fb=	622	psi	ktheta*ftheta
F'b=	1911.52		FbCdCf
622 < 1911.52 = OK			

b) Bending stress at tangent point

Mt=	49170	wl(lt)/2 - wlt^2/2
fbt=	1080	6Mt/bdt^2
F'b=	2002.55	F'b * Cd
1080 < 2002.54 = OK		

c) Radial stress at centerline

frt=	31.8	psi	KrCrf0
F'rt=	67.08	psi	
31.83 < 67.08 = OK			



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5/20/2019

DCSPE# 7196

LOCATION Mercer Island, WA

BLDG CODE

BLDG CATEGORY

Shelter Length

Shelter Width

Shelter Mean Roof Height

ASCE 7-10

Roof Dead Load

Roof Live Load

98040

2018

II

40.0 ft

20.0 ft

15.0 ft

12.0 psf

30.0 psf

SNOW DESIGN DATA

Ground Snow Load (Pg)

20.0 psf

Snow Exposure Factor (Ce)

1.0

Snow Importance Factor (Is)

1.00

Snow Thermal Factor (Ct)

1.2

Flat Roof Snow Load (Pf)

24.0 psf

Roof Slope (Cs)

1.0

Sloped Roof Snow Load (Ps)

24.0 psf

shingles

WIND DESIGN DATA

Basic Wind Speed (3-sec gust)

110 mph

Wind Importance Factor (Iw)

1.00

Wind Exposure Category

C

Internal Pressure Coefficient

0.0

Components & Cladding Wind Pressures

Z1

-12.1 psf

Z2

-22.8 psf

Z3

-34.9 psf

qh =

22.38

Wind Base Shears

Vxx

2.9 kips

Vyy

1.5 kips



SEISMIC DESIGN DATA

Seismic Importance Factor (Ie)	1.00	
Short Period Spectral Response Accel (Ss from maps)	1.443	
1-Sec Period Spectral Response Accel (S1 from maps)	0.488	
Seismic Site Class	D	
Design Short Period Spectral Response Accel (Sds)	0.96	0.66667
Design 1-sec Period Spectral Response Accel (Sd1)	0.49	
Seismic Design Category	D	
Basic Seismic Resisting System	CANTILEVERED COLUMN SYSTEM	
Basic Seismic Force Resisting System	TIMBER FRAMES	
Response Modification Factor (R)	1.5	
Seismic Response Coefficient (Cs)	0.64	
Seismic Base Shear (Allowable Stress Design)	7.20	kips

